Effect of high-$n$ and continuum eigenstates on the Stark effect of resonance lines of atoms and ions

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We investigate the Stark effect for spectral transitions between low-lying levels of atoms and ions. We find that often a strong cancellation of the shifts of the lower and upper levels occurs, resulting in a significant reduction in the shift. For accurate calculations, therefore, one has to account for the influence of high-principal-quantum-number states. As examples, the shifts, splitting, and intensities of the components of the Li I 2s-2p, Na I 3s-3p, Ba II 5d-6p, Ba II 6s-6p, and the quadrupole Ba II 6s-5d (shifts only) transitions are calculated for electric fields up to $\approx 20$ MV/cm. Comparison of the calculated shift parameters to experimental data for the Li I 2s-2p, Na I 3s-3p, and Ba II 6s-5d lines, available as yet only for low fields for which the effect is quadratic, showed an excellent agreement for most of these lines. [S1050-2947(97)02610-3]

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I. INTRODUCTION

The investigation of emission patterns of atoms under electric fields is important for the diagnostics of numerous phenomena in plasma physics. The recent advances in high voltage technology allow electric fields up to 10 MV/cm to be produced in the laboratory [1–4]. Knowledge of the level energy shifts under high fields allows the electric field distribution to be obtained from line-emission patterns, as has been done for fields $\approx 1$ MV/cm [5], using the 4$p$–4$d$ transitions in Al III, and $\approx 10$ MV/cm [6], using the 2$s$–2$p$ transitions in Li I. For the determination of the electric fields in such studies, line-shift calculations accurate to within a very few percent are required. Here, we demonstrate that the Stark shift parameters for both the ground and first excited states are often of the same order and cancel each other to a large extent. Thus an accurate calculation of the shifts of these levels requires accounting for the effects of high-lying levels including those of the continuous spectrum. The effect of high-lying levels on the electric-field-induced shift parameters can be large when both upper and lower levels of the transition are energetically separated from the other levels, i.e., not only for principal resonance lines (for example, transitions between the 5$d$ and 6$p$ levels in Ba II, see below). Neglecting the contribution of the high levels may thus lead to significant errors in the calculations.

II. CALCULATION PROCEDURE

We use the $n,l,m_l,m_s$ representation. The Hamiltonian is of the form

$$H = H_0 + V_{ls} + V_{EF},$$  (1)

where $H_0$ is the Hamiltonian due to the Coulomb interaction ($H_0$ is diagonal, giving the energy levels with no $ls$ interaction), $V_{ls}$ is the perturbation due to the $ls$ coupling, and $V_{EF}$ is the perturbation due to the electric field. Here,

$$V_{ls} = A_{nl} \vec{F} \cdot \vec{s},$$  (2)

where $A_{nl}$ are constants derived from atomic level data tables (e.g., [7]), and

$$V_{EF} = -eFz,$$  (3)

where the electric field $\vec{F}$ is assumed to be in the $z$ direction.

The matrix elements of Eqs. (2) and (3) can be written as

$$\langle n'l'm'_l|m'_{ls}|V_{ls}|nlm_{ls}\rangle = (A_{nl}/2)\delta_{n'n}\delta_{l'l}\delta_{m_l'-m_l+1}\delta_{m_{s'}}1\delta_{m_l,m_l+1}$$
$$\times \sqrt{(l-m_l)(l+m_l+1)}$$
$$+ \delta_{m_{s'},1}\delta_{m_{s'},1}\delta_{m_{s},m_{s}}\sqrt{(l+m_l)(l-m_l+1)}$$
$$+ 2\delta_{m_{s'},1}\delta_{m_{s},m_{s}}$$  (4)

and

$$\langle n'l'm'_l|m'_{ls}|V_{EF}|nlm_{ls}\rangle = -iea_F(-1)^{l'-m'}$$
$$\times \begin{pmatrix} l' & 1 & l \\ -m' & 0 & m \end{pmatrix} \langle n'l'|r|nl \rangle.$$  (5)

The absolute values of the reduced matrix elements $(n'l'|r|nl)$ are derived from the oscillator strengths $f$ for absorption of the corresponding transitions:

$$\langle n'l'|r|nl \rangle = \sqrt{3f_{ik}R(2l+1)} / E_i - E_k.$$  (6)

where $R$ is the Rydberg constant and $E_i$ and $E_k$ are the energies of the upper and lower levels, respectively. The signs of the matrix elements, which are important for the nonquadratic Stark effect, are taken from matrix elements calculated using the code due to Cowan [8], based on the Hartree-Fock method with relativistic corrections (here called the HFR method).
In order to limit the number of levels in the Hamiltonian matrix, we identified the levels the effect of which is very close to quadratic. These levels include the discrete levels with high principal quantum numbers and the continuum levels. The effect of those levels could be replaced by the effect of a few “effective” levels.

Thus the Hamiltonian matrix includes the levels taken explicitly, and, in addition, it includes the effective levels \( \vec{s}_i, \vec{p}_i, \vec{d}_i, \ldots \) (one level for each value of the orbital momentum that can mix with either the initial or final levels of the transition under investigation), which replace all higher levels (the discrete and the continuum ones) as stated above.

After the diagonalization of the Hamiltonian, the radii-vector matrix elements, calculated in the basis of the new wave functions, give the intensities of spectral line components in the dipole approximation.

For the sake of comparison with other studies, we also give in this paper the quadratic Stark effect parameters \( \gamma \), obtained in our calculations by taking the low-field limit through the relation

\[
\Delta E = \gamma F^2. \tag{7}
\]

III. THE EFFECT OF THE HIGH LEVELS

As said above, we identified the discrete and the continuum levels that are high enough to cause an almost purely quadratic Stark shift of the levels concerned for the electric field range addressed. These levels are replaced by the effective levels \( \vec{\alpha}_i \). The oscillator strength \( f_{\vec{\alpha}_i} \) between a low-lying level \( i \) with an energy \( E_i \) and the effective level \( \vec{\alpha} \) with an energy \( E_{\vec{\alpha}} \) can be calculated using the following identity:

\[
\frac{f_{\vec{\alpha}i}}{(E_i - E_{\vec{\alpha}})^2} = \sum_k \frac{f_{ik}}{(E_i - E_k)^2} + \int dE \frac{d f/dE}{(E_i - E)^2}, \tag{8}
\]

where the summation and integration, respectively, are carried out over the high discrete levels and the continuum levels that are replaced by the effective levels.

The transition probability between the level \( i \) and the discrete levels that are close to the continuum region is proportional to the energy level density, i.e., to \( 1/n^3 \). Therefore, for high \( n \), \( f_{ik} \) can be assumed to obey

\[
f_{ik} = \frac{\lambda_i}{n^3}. \tag{9}
\]

The coefficients \( \lambda_i \) are obtained from the HFR-code calculations for \( n \) varying within an appropriate range of high values and taking limits of the series. The uncertainties in the coefficients due to this procedure cause no significant error in the calculation of the total quadratic Stark effect since the contribution of the high-\( n \) discrete levels is small compared to that of the continuum levels. This is shown in Table I for Li I, where the quadratic constants \( \gamma \) due to the high-\( n \) discrete levels and due to the continuum levels are given separately.

The values of \( d f/dE \) for the continuous-spectrum wave functions are calculated by the HFR code. The energies of the effective levels \( E_{\vec{\alpha}} \) can be chosen arbitrarily, provided they are chosen to be high enough to satisfy the assumption of a pure quadratic Stark effect.

The energy levels \( E_{\vec{\alpha}} \) and the oscillator strengths \( f_{\vec{\alpha}i} \) thus obtained are used in the Hamiltonian matrix, in order to replace all high-\( n \) discrete levels and continuum levels.

IV. AVOIDED CROSSINGS

In calculating the Stark effect for strong electric fields, the problem of avoided crossings has to be treated properly. For high fields the Rydberg levels can be shifted close to the levels under investigation. This can strongly affect the shifts of the lower levels, if they mix with the Rydberg levels. As a very simplified example, let us consider the following effective two-level Hamiltonian:

\[
H = H_0 + V, \tag{10}
\]

with

\[
H_0 = \begin{pmatrix} E_{Ry} & 0 \\ 0 & E_0 \end{pmatrix} \quad \text{and} \quad V = \begin{pmatrix} -\alpha F & \beta F \\ \beta F & \gamma F^2 \end{pmatrix}. \tag{11}
\]

Here, \( E_0 \) and \( E_{Ry} \) are the unperturbed energies of the lower level and the Rydberg level, respectively. \( \alpha \) gives the linear shift of the Rydberg state, \( \beta \) gives the mixing between the two levels, and \( \gamma \) is the coefficient of the quadratic Stark effect for the lower level due to the interaction with the rest of the atomic levels (this is what we mean by “effective two-level Hamiltonian”). For \( \alpha, \beta, \) and \( \gamma \) satisfying

\[
\frac{\beta}{\alpha} \ll 1; \quad \frac{\gamma(E_{Ry} - E_0)}{\alpha^2} \ll 1,
\]

the distance between the levels approaches its minimal value of \( \approx 2(\beta/\alpha)(E_{Ry} - E_0) \) at the electric field \( F_0 = (E_{Ry} - E_0)/\alpha \). Near this point the shifts and intensities vary sharply as a function of the electric field. However, one has to consider the Rydberg-level field ionization at electric fields lower than \( F_0 \). If this happens, the Rydberg state joins the continuum, making this picture unrealistic. In the calculations, it is possible to avoid this problem by preventing the Rydberg levels from splitting linearly for fields larger than the field-ionization threshold. This is made in our calculations by forcing the radius-vector matrix elements between different sublevels with the same principal quantum number to be 0 at electric fields exceeding the ionization threshold of these levels. These thresholds were determined by the semiclassical method ([12], and references therein).

<table>
<thead>
<tr>
<th>Level</th>
<th>( \gamma ) due to the continuum levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>( 2s_1/2,1/2 )</td>
<td>(-1.58(-4))</td>
</tr>
<tr>
<td>( 2p_{1/2,1/2} )</td>
<td>(-4.49(-3))</td>
</tr>
<tr>
<td>( 2p_{3/2,1/2} )</td>
<td>(-5.22(-3))</td>
</tr>
<tr>
<td>( 2p_{3/2,3/2} )</td>
<td>(-3.75(-3))</td>
</tr>
</tbody>
</table>
TABLE II. Values of the total $\gamma$ [cm$^{-1}$/MV/cm$^2$] and of $\gamma$ only due to the high-$n$ and the continuum levels for the Li I 2$s$ and 2$p$ levels.

<table>
<thead>
<tr>
<th>Level</th>
<th>Total $\gamma$</th>
<th>$\gamma$ due to the high-$n$ and the continuum levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>2$s_{1/2,1/2}$</td>
<td>−0.680</td>
<td>−5.04(−3)</td>
</tr>
<tr>
<td>2$p_{1/2,1/2}$</td>
<td>−0.526</td>
<td>−3.46(−2)</td>
</tr>
<tr>
<td>2$p_{3/2,1/2}$</td>
<td>−0.518</td>
<td>−4.05(−2)</td>
</tr>
<tr>
<td>2$p_{3/2,3/2}$</td>
<td>−0.533</td>
<td>−2.87(−2)</td>
</tr>
</tbody>
</table>

V. RESULTS

A. Li I transitions

The oscillator strengths of the Li I 2$s$-2$p$ and 2$p$-3$s$ transitions are taken from Ref. [9], of the 2$p$-3$d$ from Ref. [10], and all others between levels up to $n = 10$ are taken from Ref. [11].

The quadratic-effect constants $\gamma$ for the levels and for the transitions are given in Tables II and III, respectively. In both tables, the left columns give the total values of $\gamma$ and the right columns give the values due to the high-$n$ discrete levels and the continuum levels. One can see that the contributions of these levels to the shifts of the upper or lower levels of the 2$s$-2$p$ transition are less than 8%. However, due to the strong cancellation of the 2$s$ and 2$p$ shifts, the contributions of the high levels to the shifts of the transition components reach $\approx$20% (in fact, they only reach $\approx$20%, in spite of the strong cancellation, since the cancellation also occurs for the high-level contributions, as can be inferred from Table II).

The calculated Stark shifts for the 2$s$-2$p$ transitions of Li I as a function of the electric field are shown by the solid lines in Fig. 1. Intensities of the different components of the line as a function of the electric field are given by the solid lines in Fig. 2. In the figures, note the crossing of the energy levels at a field $\approx$8.5 MV/cm, which breaks the monotonous behavior of the component intensities. The crossing of the energy levels is caused by the deviation of the Stark effect from the quadratic one.

To illustrate the importance of the nonquadratic Stark effect we also calculate the shift and intensities assuming a pure quadratic effect for all levels. This was implemented by substituting all levels, except for the 2$p$ and 2$s$ levels, by three effective levels that give the quadratic Stark shift constants $\gamma$, using the method described in Sec. III. The results are shown by the dashed lines in Figs. 1 and 2 (the dashed curves differ from pure parabolas with constants $\gamma$ due to the $ls$ interaction). The significant deviations of the intensities at fields above 5 MV/cm and of the shifts at fields above 10 MV/cm from the quadratic behavior are seen.

The present calculations of the quadratic effect can be compared to the calculations given in Ref. [13]. The difference is about 100% for the shift constants of the transition components. It is possible that in Ref. [13] the contribution of the continuum levels was not taken into account. However, based on the present calculations, this neglect can only account for a discrepancy of $\approx$20% between the two calculations.

There are other theoretical calculations of the Li I Stark parameters performed using different techniques. In Ref. [14] only presented is the quadratic-effect constant for the Li I $D_1(2s_{1/2}-2p_{1/2})$ line, which coincides with ours to

TABLE III. Values of the total $\gamma$ [cm$^{-1}$/MV/cm$^2$] and of $\gamma$ only due to the high-$n$ and the continuum levels for the Li I 2$s$-2$p$ transitions.

<table>
<thead>
<tr>
<th>Transition</th>
<th>Total $\gamma$</th>
<th>$\gamma$ due to the high-$n$ and the continuum levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>2$s_{1/2,1/2}$-2$p_{1/2,1/2}$</td>
<td>0.154</td>
<td>−2.96(−2)</td>
</tr>
<tr>
<td>2$s_{1/2,1/2}$-2$p_{3/2,1/2}$</td>
<td>0.162</td>
<td>−3.55(−2)</td>
</tr>
<tr>
<td>2$s_{1/2,1/2}$-2$p_{3/2,3/2}$</td>
<td>0.147</td>
<td>−2.37(−2)</td>
</tr>
</tbody>
</table>
within 0.5%. It is of special interest, however, to compare our results to calculations for high fields. In this respect, the only study known to us is that given in Ref. [15]. For an electric field of 10 MV/cm the differences are ≈25% and 15% for the 2s0-2p0 and 2s0-2p±1 components of the line. For an electric field of 15 MV/cm the differences are ≈35% and 5%, respectively. For fields much lower than 10 MV/cm, the comparison between the results of Ref. [15] and our study is not possible, since in Ref. [15] the fine coupling (that is important for such fields) was neglected.

Due to the strong cancellation of the redshifts and blueshifts, the uncertainties in the oscillator strengths cause large errors in the total shift. For example, an error of 1% in the oscillator strength of the 2s-2p transition produces an error of 6% in the total shift. However, the 2s-2p, 2p-3s, and 2p-3d oscillator strengths were calculated with a high accuracy. The uncertainties for the first two are believed to be <0.1%, and for the third one better than 0.5% [9,10]. Therefore these uncertainties are expected to affect the accuracy in our calculations by less than 1%. The other important transitions are the 2p-nd transitions that contribute about 75% of the total shift. The oscillator strengths of these transitions differ from the hydrogenic ones by less than 10%. We believe, therefore, that their calculated values are accurate to within a few percent. Thus, accounting for the uncertainties of all oscillator strengths that affect the 2s-2p line shifts, we believe that the uncertainty in our line-shift calculations is ≈5%.

However, in spite of the uncertainties in the oscillator strengths, the present calculations appear to be rather accurate for low fields. We compare them to experimental data for fields up to 400 kV/cm obtained with an accuracy of ≈0.5% [16] and ≈0.1% [17]. For these fields the Stark shift is quadratic. Our quadratic constants for all components of the 2s-2p transition were found to agree to within <1% with the experimental ones. This good agreement could result either from a coincidental cancellation of the errors in the oscillator strengths or from accuracies in the oscillator strength calculations that are better than quoted above.

B. Na I transitions

Here, levels with \( n \leq 10 \) were included explicitly. For the levels with principal quantum number up to 6 we used the oscillator strengths given in Ref. [18], and for the other levels we used the calculations given in Ref. [11].

The calculated Stark shifts for the 3s-3p transitions in Na I are shown as a function of the electric field in Fig. 3, and the intensities of the different components of the line are given in Fig. 4. The Stark effect for this Na I line deviates from a quadratic behavior (not shown in Fig. 3) for fields lower than for Li I; the deviation is about 10% at 2 MV/cm and >100% at 10 MV/cm.

Calculated values for the quadratic effect for the 3s and 3p levels are given in Table IV and the values of the quadratic Stark shift parameters for the Na I 3s-3p line components are given in Table V. Comparison of the quadratic-shift parameters given in Table V with precise measurements [19] for fields up to 150 kV/cm shows an agreement to within 1%. It is also seen in Table V that the contribution of the high-\( n \) and continuum levels to the total line shifts is less than 2%, i.e., the relative contribution of these levels is lower than for Li I.

C. Ba II transitions

The oscillator strengths between levels with the principal quantum number up to 12, used to calculate the Stark effect

![Image](https://example.com/image1.png)

**FIG. 3.** The Stark shifts of the Na I 3s-3p line components as a function of the electric field.

![Image](https://example.com/image2.png)

**FIG. 4.** Intensities of the Na I 3s-3p line components as a function of the electric field. The observation direction is perpendicular to the electric field. The solid line corresponds to the 3s_{1/2}→3p_{1/2} component and the dashed lines correspond to the 3s_{3/2}→3p_{3/2} components.

**TABLE IV.** Values of the total \( \gamma [\text{cm}^{-1}/(\text{MV/cm})^2] \) and of \( \gamma \) only due to the high-\( n \) and the continuum levels for the Na I 3s and 3p levels.

<table>
<thead>
<tr>
<th>Level</th>
<th>Total ( \gamma )</th>
<th>( \gamma ) due to the high-( n ) and the continuum levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>3s_{1/2,1/2}</td>
<td>−0.671</td>
<td>−3.1(−4)</td>
</tr>
<tr>
<td>3p_{1/2,1/2}</td>
<td>−1.498</td>
<td>−2.6(−2)</td>
</tr>
<tr>
<td>3p_{3/2,3/2}</td>
<td>−1.865</td>
<td>−3.1(−2)</td>
</tr>
<tr>
<td>3p_{3/2,3/2}</td>
<td>−1.136</td>
<td>−2.0(−2)</td>
</tr>
</tbody>
</table>
TABLE V. Values of the total $\gamma$ [cm$^{-1}/$(MV/cm)$^2$] and of $\gamma$ only due to the high-$n$ and the continuum levels for the Na I 3s-3$p$ transitions.

<table>
<thead>
<tr>
<th>Transition</th>
<th>Total $\gamma$</th>
<th>$\gamma$ due to the high-$n$ and the continuum levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>3$s_{1/2}$-3$p_{1/2}$</td>
<td>-0.827</td>
<td>-2.6(-2)</td>
</tr>
<tr>
<td>3$s_{1/2}$-3$p_{3/2}$</td>
<td>-1.194</td>
<td>-3.1(-2)</td>
</tr>
<tr>
<td>5$s_{1/2}$-3$p_{3/2}$</td>
<td>-0.465</td>
<td>-2.0(-2)</td>
</tr>
</tbody>
</table>

of Ba II lines, were taken from [11] except those for the 6$s$-6$p$ and 5$d$-6$p$ transitions for which the recently measured values [20] were used.

Figure 5 presents the Stark shifts of the Ba II 6$s$-6$p$ transitions. We do not show intensities of the Ba II 6$s$-6$p$ transition components because they do not deviate from their zero-field values by more than 2% even for electric field of 20 MV/cm. Figures 6–8 and 9, respectively, give the Stark zero-field values by more than 2% even for electric field of more than 2% even for electric field of 20 MV/cm. Figures 6–8 and 9, respectively, give the Stark zero-field values.

In the calculations described above, the effect of the magnetic field on the line splitting can be easily accounted for.

VI. THE EFFECT OF MAGNETIC FIELD

In the calculations described above, the effect of the magnetic field on the line splitting can be easily accounted for.
Here, \( \sim \) corresponds to the perpendicular to the electric field. The solid, dashed, and dot-dashed lines function as a function of the electric field. The observation direction is perpendicular to the electric field.

To this end, we modify the formula (1) to

\[
H = H_0 + V_{ls} + V_{EF} + V_{MF},
\]

(10)

where \( V_{MF} \) is the perturbation due to the magnetic field \( \vec{B} \) and can be expressed as

\[
V_{MF} = \mu \vec{B} \cdot (\vec{I} + g_e \vec{s}).
\]

(11)

Here, \( \mu \) is the Bohr magneton and \( g_e \) is the \( g \) factor of the electron.

The matrix elements of Eq. (11) can be written as

\[
\langle n' l' m'_l m'_s | V_{MF} | n l m_s \rangle = (\mu/2) g_e \delta_{nn'} \delta_{ll'} (B_x - iB_y) \times [\delta_{m_l',m_l+1}(l-m_l)(l+m_l+1) + \delta_{m_l',m_s+1}g_e] + (B_x + iB_y) \delta_{m_l',m_l-1}(l+m_l)(l-m_l+1) + \delta_{m_l',m_s-1}g_e + 2B_y (\delta_{m_l',m_l} + \delta_{m_s',m_s}g_e m_s). \]

(12)

This modification allows one to calculate the emission pattern of the spectral lines under the combined effects of electric and magnetic fields.

VII. SUMMARY

The importance of the effect of the high-principal quantum-number and continuum levels on the shift and splitting of spectral patterns of transitions between low-lying levels of atoms and ions is shown. This becomes important due to the high-\( n \) and the continuum levels for the Ba II 6s, 5d, and 6p levels.

**TABLE VI.** Values of the total \( \gamma \) [cm\(^{-1}\)/(MV/cm)] and of \( \gamma \) only due to the high-\( n \) and the continuum levels for the Ba II 6s, 5d, and 6p levels.

<table>
<thead>
<tr>
<th>Level</th>
<th>Total ( \gamma )</th>
<th>( \gamma ) due to the high-( n ) and the continuum levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>6s( _{1/2,1/2} )</td>
<td>-0.457</td>
<td>-7.0 (-5)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )</td>
<td>-0.060</td>
<td>-4.3 (-3)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )</td>
<td>-0.025</td>
<td>-3.8 (-3)</td>
</tr>
<tr>
<td>6p( _{1/2,1/2} )</td>
<td>-0.049</td>
<td>-6.4 (-3)</td>
</tr>
<tr>
<td>6p( _{3/2,3/2} )</td>
<td>-0.137</td>
<td>-4.6 (-3)</td>
</tr>
</tbody>
</table>

**TABLE VII.** Values of the total \( \gamma \) [cm\(^{-1}\)/(MV/cm)] and of \( \gamma \) only due to the high-\( n \) and the continuum levels for the Ba II 6s-6p and 5d-6p transitions.

<table>
<thead>
<tr>
<th>Transition</th>
<th>Total ( \gamma )</th>
<th>( \gamma ) due to the high-( n ) and the continuum levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>6s( _{1/2,1/2} )-6p( _{1/2,1/2} )</td>
<td>0.408</td>
<td>-6.3 (-3)</td>
</tr>
<tr>
<td>6s( _{1/2,1/2} )-6p( _{3/2,1/2} )</td>
<td>0.396</td>
<td>-8.4 (-3)</td>
</tr>
<tr>
<td>6s( _{1/2,1/2} )-6p( _{3/2,1/2} )</td>
<td>0.320</td>
<td>-4.5 (-3)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )-6p( _{1/2,1/2} )</td>
<td>0.195</td>
<td>7.0 (-4)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )-6p( _{3/2,1/2} )</td>
<td>0.011</td>
<td>-2.1 (-3)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )-6p( _{3/2,1/2} )</td>
<td>0.183</td>
<td>-1.4 (-3)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )-6p( _{3/2,1/2} )</td>
<td>-0.001</td>
<td>-4.2 (-3)</td>
</tr>
<tr>
<td>5d( _{1/2,1/2} )-6p( _{3/2,3/2} )</td>
<td>0.107</td>
<td>2.5 (-3)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )-6p( _{3/2,1/2} )</td>
<td>-0.077</td>
<td>-3.0 (-4)</td>
</tr>
<tr>
<td>5d( _{1/2,1/2} )-6p( _{3/2,3/2} )</td>
<td>0.185</td>
<td>-1.2 (-3)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )-6p( _{3/2,1/2} )</td>
<td>0.112</td>
<td>-2.3 (-3)</td>
</tr>
<tr>
<td>5d( _{1/2,1/2} )-6p( _{3/2,3/2} )</td>
<td>0.109</td>
<td>2.7 (-3)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )-6p( _{3/2,1/2} )</td>
<td>0.036</td>
<td>1.6 (-3)</td>
</tr>
<tr>
<td>5d( _{3/2,3/2} )-6p( _{3/2,1/2} )</td>
<td>-0.112</td>
<td>-8.0 (-4)</td>
</tr>
</tbody>
</table>
to a strong cancellation of the shifts of the lower and upper levels, resulting in a significant reduction in the line shift that consequently increases the influence of the high levels. The shifts and intensities of the Stark components of a few spectral lines were calculated for electric fields up to $\approx 20$ MV/cm. The calculated shift parameters are in very good agreement with experimental measurements, as yet only available for low fields.

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<table>
<thead>
<tr>
<th>Transition</th>
<th>Present calculations</th>
<th>Experiment</th>
</tr>
</thead>
<tbody>
<tr>
<td>$6s_{1/2,1/2} - 5d_{5/2,1/2}$</td>
<td>0.211</td>
<td>0.20±0.02</td>
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<tr>
<td>$6s_{1/2,1/2} - 5d_{3/2,3/2}$</td>
<td>0.284</td>
<td>0.25±0.03</td>
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<tr>
<td>$6s_{1/2,1/2} - 5d_{5/2,5/2}$</td>
<td>0.432</td>
<td>0.39±0.04</td>
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</table>